

# APPORT DE LA MODÉLISATION MOLÉCULAIRE À LA COMPRÉHENSION DU COMPORTEMENT THERMODYNAMIQUE DES FLUIDES CONFINÉS

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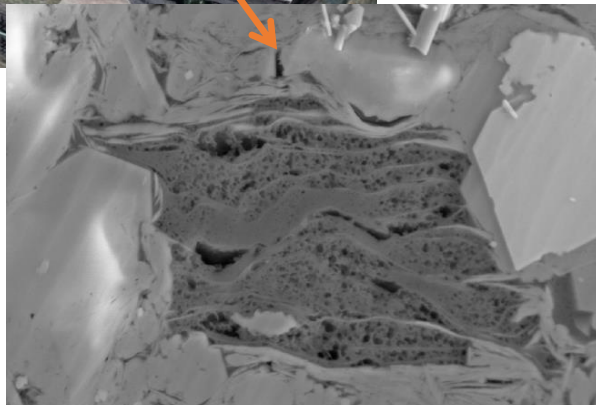
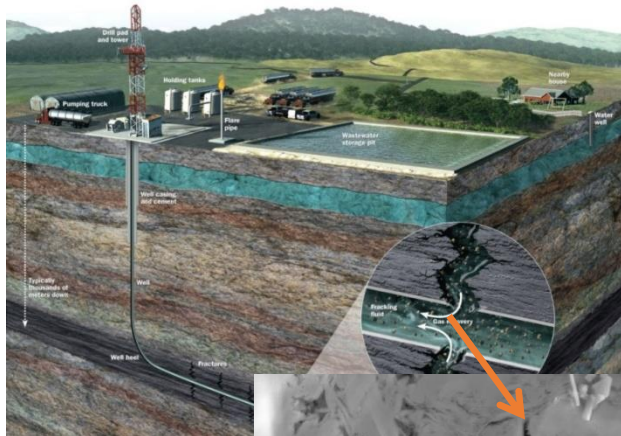
CARLOS NIETO-DRAGHI



JTSS: Journée Thermodynamique du Sous-Sol SFGP 12 juillet 2022 Pau

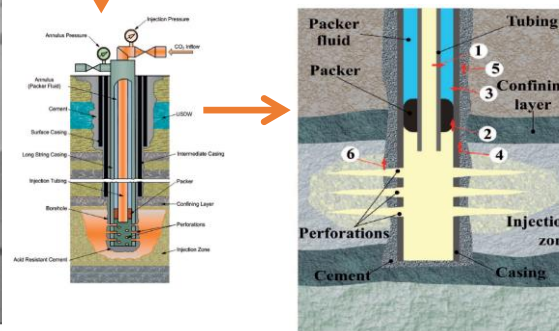
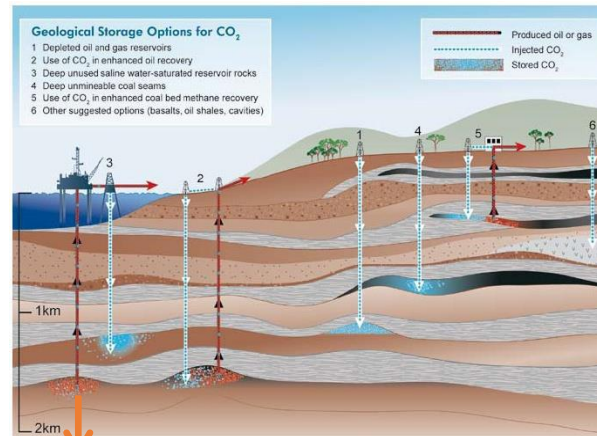
# CONTEXT OF APPLICATIONS (I)

- Understand the phase behavior of fluids under confinement or adsorbed at mineral surfaces
- Problem can be present in different applications: Shale reservoirs, CCS, soil decontamination

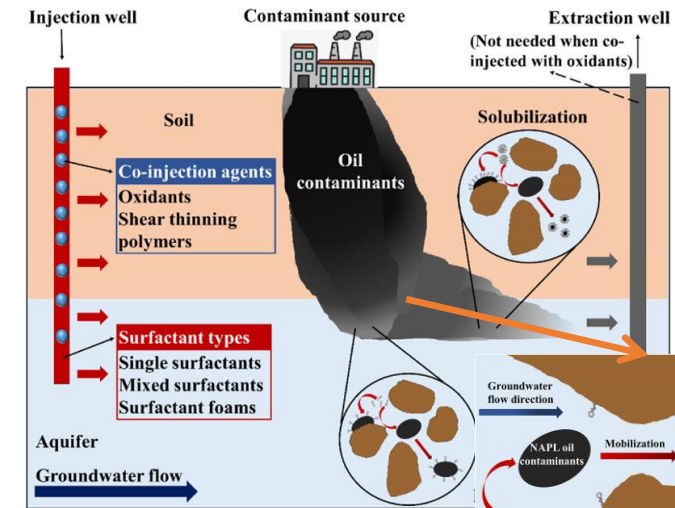


1 μm EHT = 5.00 kV Signal A = SE2 Date : 5 Oct 2007  
WD = 5 mm Mag = 10.05 K X

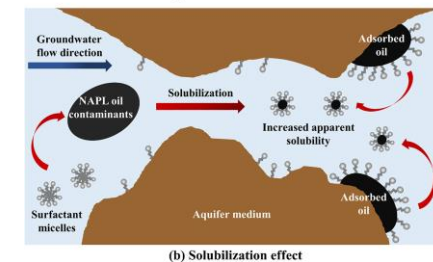
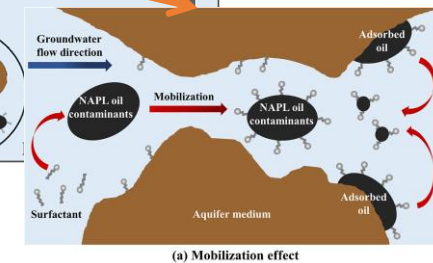
Scanning electron microimage of Barnett Shale (Wang, 2009)



Integrity of wells for CO<sub>2</sub> injection at reservoir conditions (Pasic, 2011)



Surfactant remediation of oil-contaminated soils and groundwater (Liu, 2021)



# CONTEXT OF APPLICATIONS, LENGTH SCALES VS CONFINEMENT & STATISTICAL MECHANICS

- Strong rock-fluid interaction within nano-pores at reservoir thermodynamic conditions
- Very heterogenous pore size distribution (PSD)
- Nanoscale confinement changes the PVT behavior of the fluid at small scale
- Impact on reservoir/injection/production monitoring at large scale

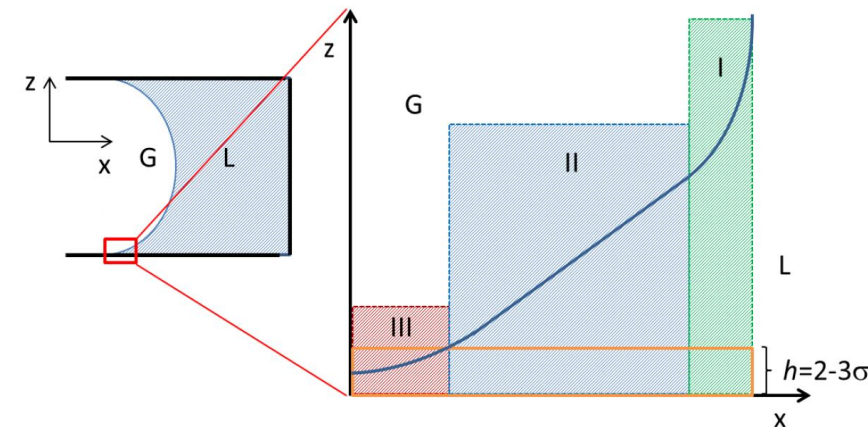
Consider materials of different porosity size (crystalline or not)

IUPAC: microporous (<2 nm), mesoporous (2-50 nm) and macroporous (>50 nm)

In macropores in contact to a LV bulk system

- I. Capillary zone → Classically handled by Laplace-Young (L-Y)
- II. Transition zone → Extension of L-Y by including the adsorbed layer though  $\Pi(h)$  (disjoining pressure vdW+elec)
- III. Molecular zone → Governed by the relative strength of adsorbate-wall vs adsorbate-adsorbate interactions

Representation of a capillary rise in contact with bulk @ LV equilibrium

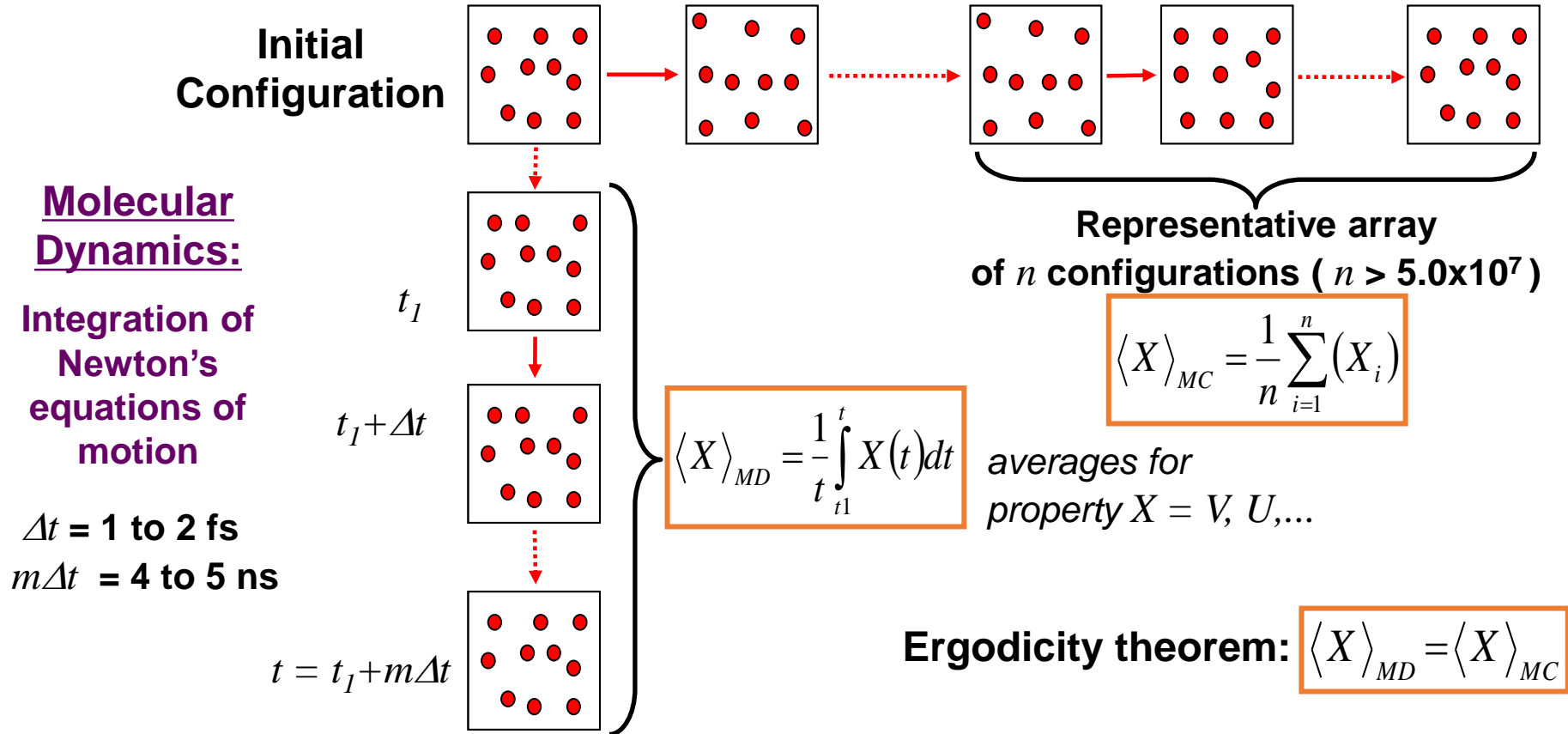


**Molecular simulation techniques are at the appropriate length scale**

**Thermodynamics ↔ Statistical mechanics**

# MOLECULAR SIMULATION TECHNIQUES

**Monte Carlo: Statistical method (Markov chain + Metropolis algorithm)**  
ensuring occurrence of configuration  $i \sim \exp(-U_i/kT)$



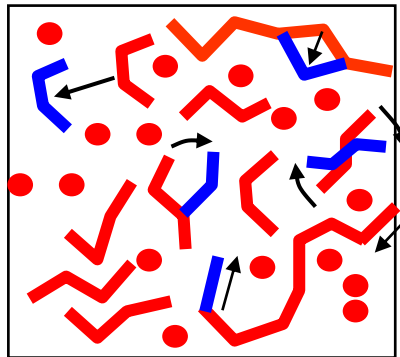
**Statistical mechanics  $\Leftrightarrow$  Thermodynamics**

# MONTE CARLO SIMULATION AT DIFFERENT ENSEMBLES

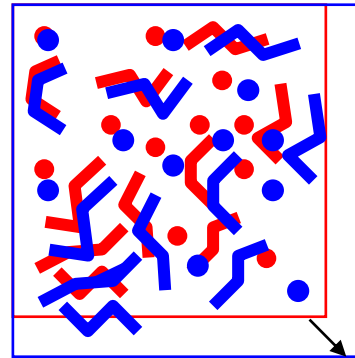
## All ensembles (NVT, NPT,...)

Internal moves (thermal equilibrium) :

Translation, rotation, reptation\*, flip, regrowth\*

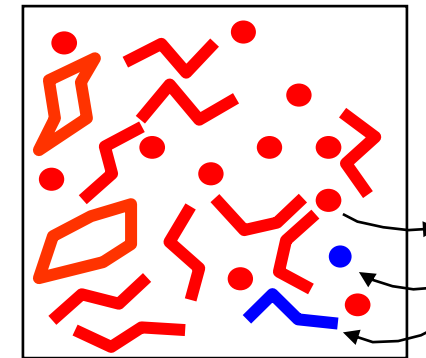


**NPT ensemble**  
volume changes  
(mechanical equilibrium at fixed pressure)



## Grand Canonical ( $\mu VT$ ) ensemble

Insertions - destructions, particle exchange (chemical equilibrium)\*



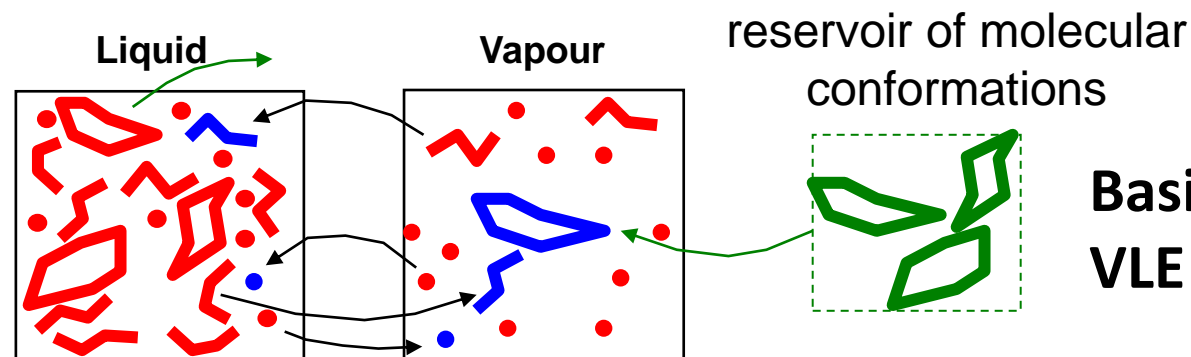
Average properties  
 $X = V, U, \dots$ , from Configurations

$$\langle X \rangle_{MC} = \frac{1}{n} \sum_{i=1}^n (X_i)$$

**Gibbs ensemble NVT (phase equilibrium without explicit interface) :**

All previous movements

Transfers between phases \*



**Basic ensemble for VLE of bulk fluids**

\* moves using statistical bias techniques such as Configurational Bias Monte Carlo[1] or reservoir bias [2]

[1] Smit et al., JCP, 1995, 102, 2126

[2] Bourasseau et al., JPC-B, 2002, 106, 5483

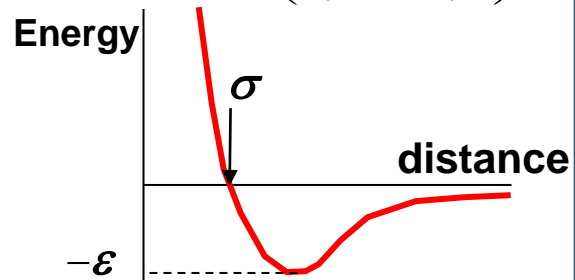


# FLUID-FLUID & WALL FLUID INTERACTIONS

## Fluid-fluid

### Lennard-Jones potentiel

$$U^{disp-rep}_{ij} = 4\epsilon \left( \frac{\sigma^{12}}{r_{ij}^{12}} - \frac{\sigma^6}{r_{ij}^6} \right)$$

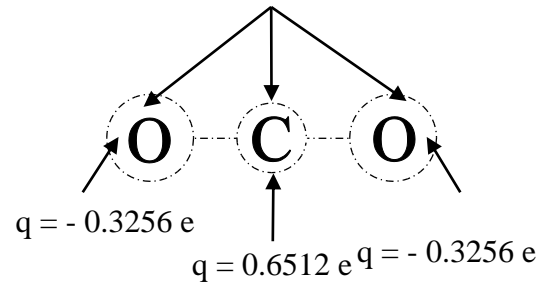


### Electrostatic energy

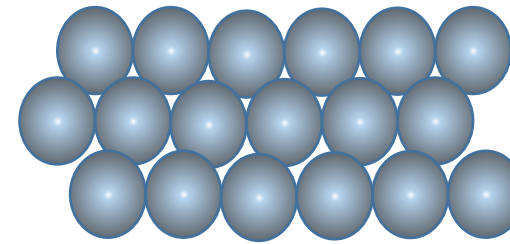
$$U^{el}_{ij} = \frac{q_i q_j}{4\pi\epsilon_o r_{ij}}$$

- Rigid molecule [1]
- Three 6-12 Lennard-Jones centers + three-point charges

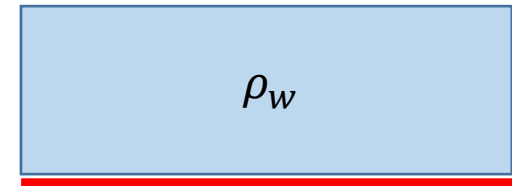
3 Lennard-Jones centers  
 ( $\sigma_O = 3.03 \text{ \AA}$  and  $\epsilon_O = 80.507 \text{ K}$ )  
 ( $\sigma_C = 2.76 \text{ \AA}$  and  $\epsilon_C = 28.129 \text{ K}$ )



## Wall-fluid [2]



Integral form

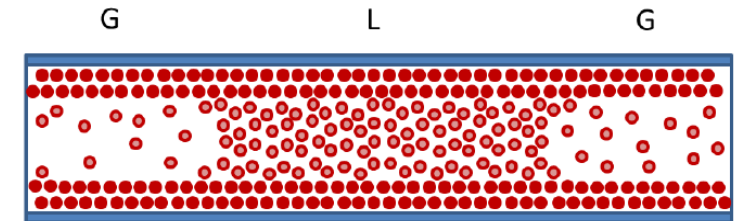


$$U_{wf} = \frac{2}{3} \pi \rho_w \epsilon_{wf} \sigma_{wf}^3 \left[ \frac{2}{15} \left( \frac{\sigma_{wf}}{z} \right)^9 - \left( \frac{\sigma_{wf}}{z} \right)^3 \right]$$

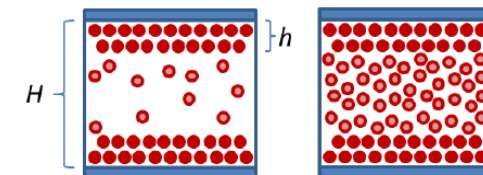
Graphite model [3] → Lorentz-Berthelot →  $\epsilon_{wf}$  &  $\sigma_{wf}$

$$U_{Tot} = U^{disp-rep} + U^{el} + U_{wf}$$

Explicit LV interface



LV without interface

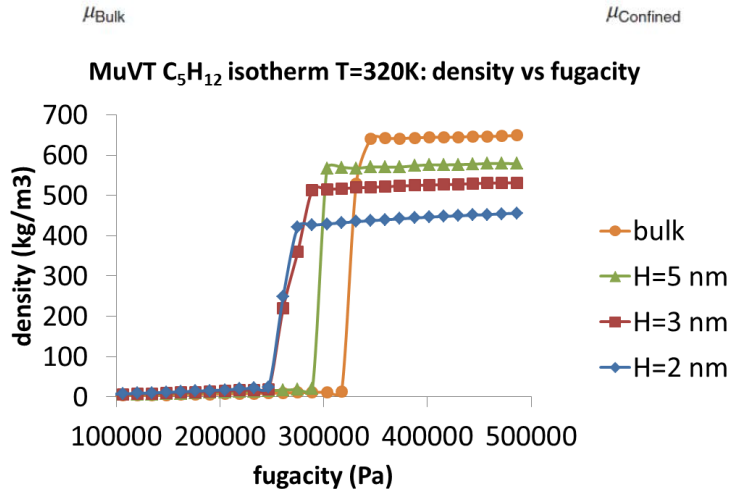
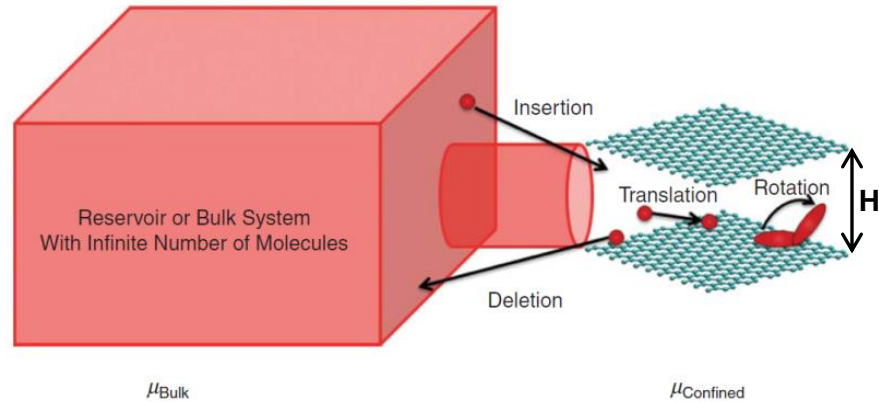


**Avoid the explicit description of the interface**

[1] Harris & Yung, J. Phys. Chem. 1995, 99, 12021  
 [2] Gelb & Gubbins Rep. Prog. Phys. 1999, 62, 1573-1659  
 [3] Porcheron et al. Phys. Chem. Chem. Phys. 1999, 1, 4083-4090

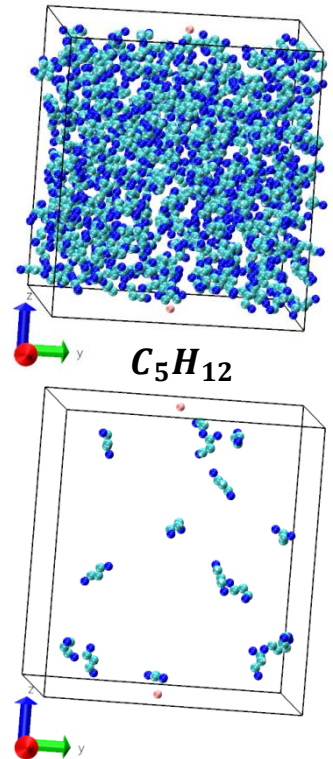
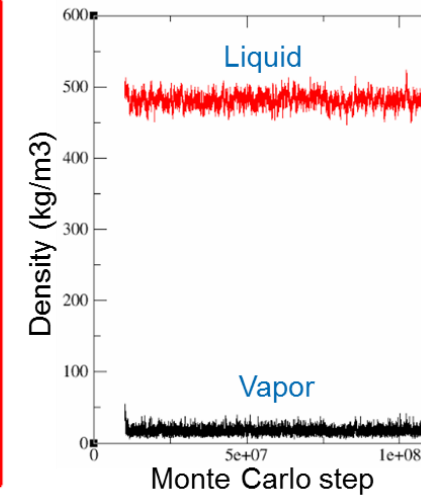
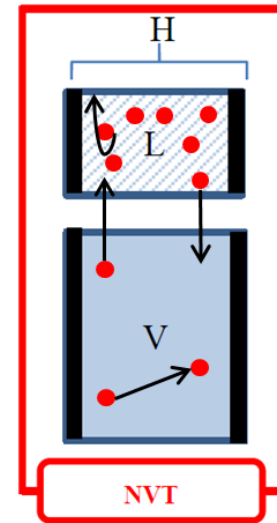
# MONTE CARLO SIMULATION OF VLE OF CONFINED FLUIDS

## ● Grand canonical Monte Carlo simulation ( $\mu VT$ )



## ● Confined Gibbs ensemble Monte Carlo simulation (NVT) [1]

Anisotropic volume change of the two boxes



Other approaches are possible:

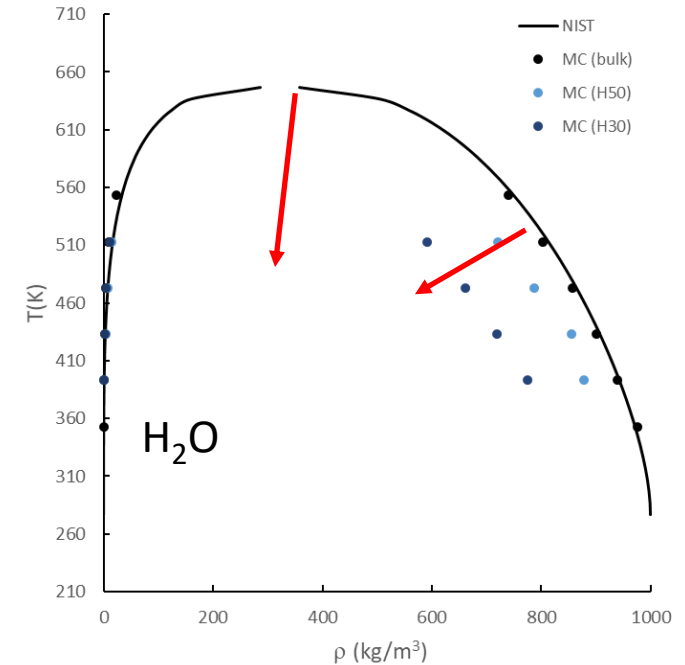
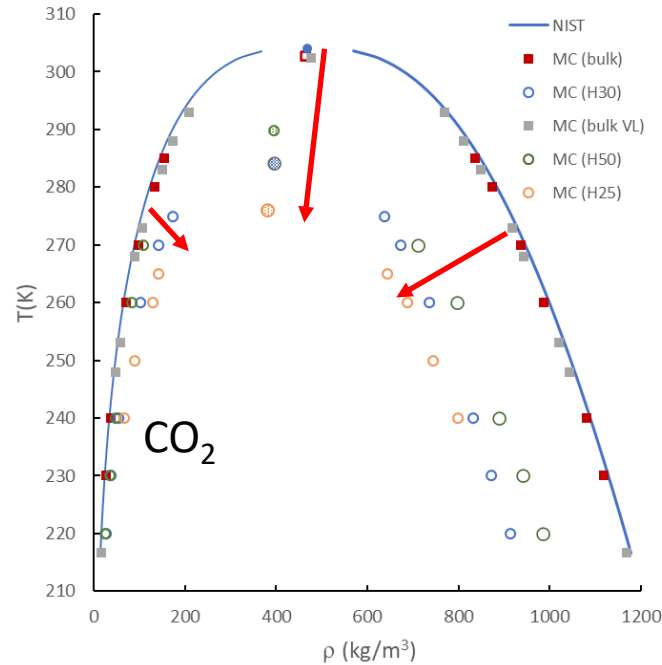
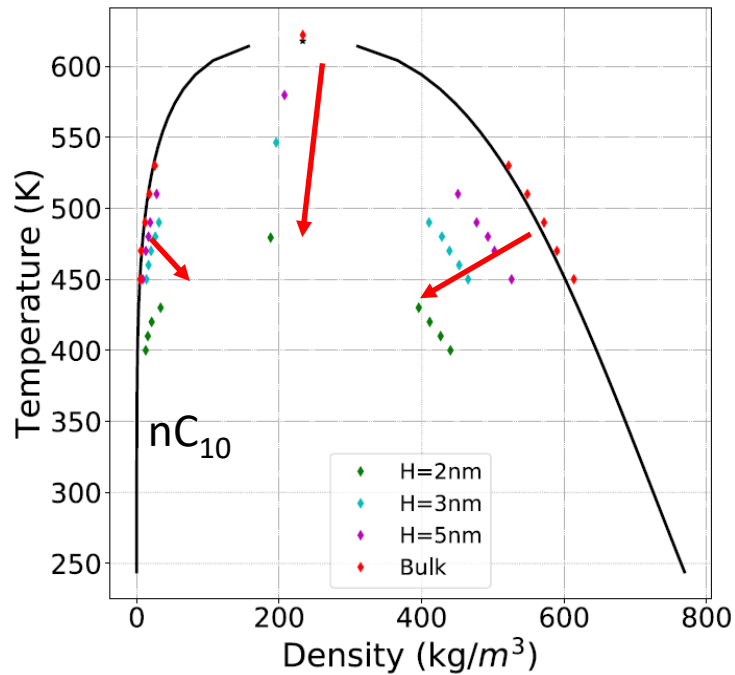
Configurational-bias grand-canonical transition-matrix Monte Carlo [2]

[1] Panagiotopoulos. Mol. Phys. 1987, 61, 813-826

[2] Errinton Phys. Rev. E. 2003, 67, 012102; J. Chem. Phys. 2003, 118, 9915

# PURE COMPONENT VLE UNDER CONFINEMENT

All fluids confined on ideal graphite slit pores

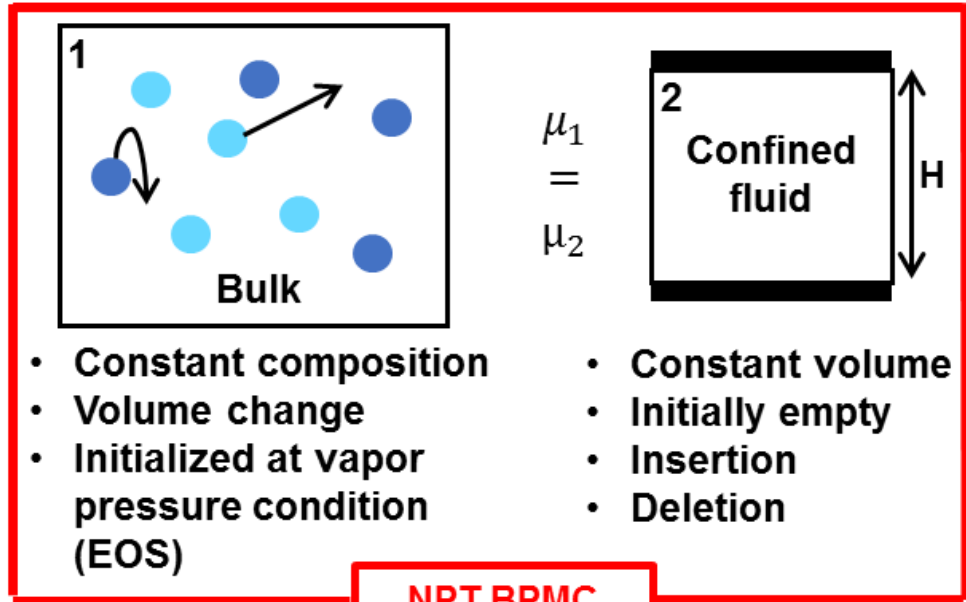


**Conclusion: Systematic reduction of the VLE with confinement**  
**→  $T_c \downarrow$  &  $P_c \downarrow$  with reduction of pore size**



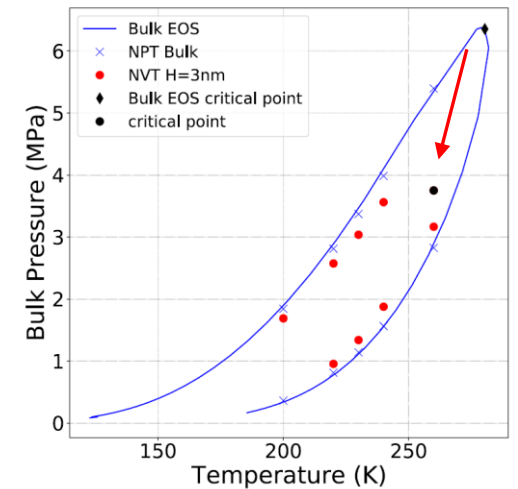
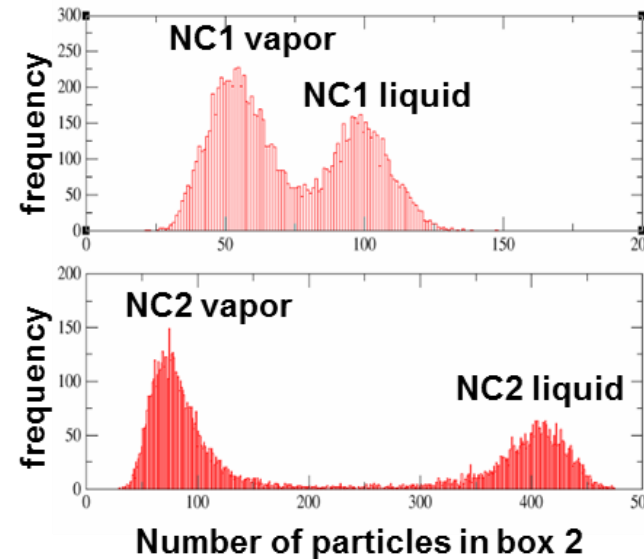
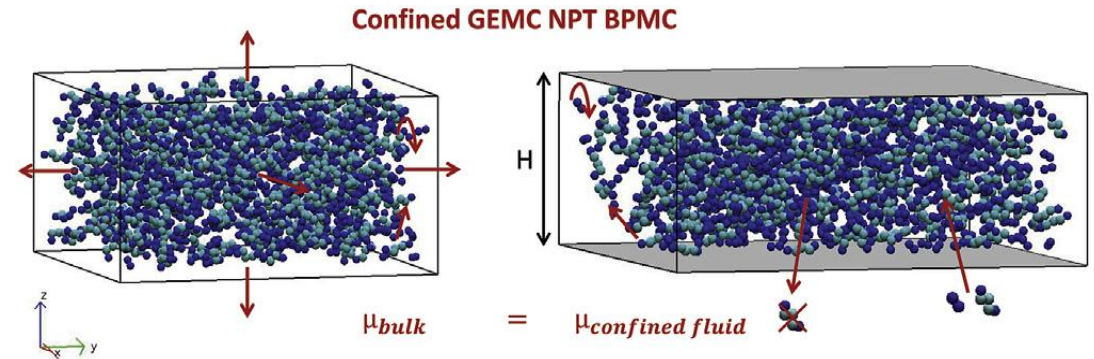
# EXTENSION TO MIXTURES: BUBBLE POINT MC SIMULATION

## Gibbs ensemble Monte Carlo simulation (NPT) with BPMC [1]



- Constant composition
- Volume change
- Initialized at vapor pressure condition (EOS)
- Constant volume
- Initially empty
- Insertion
- Deletion

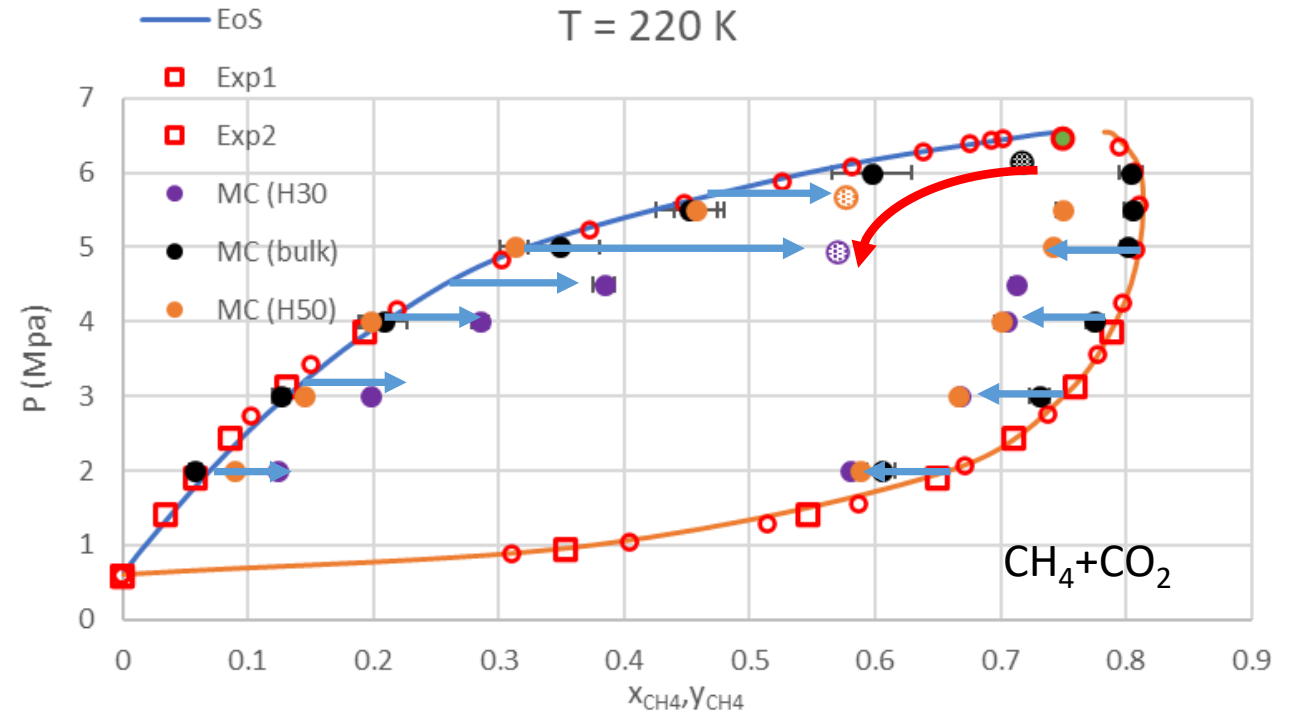
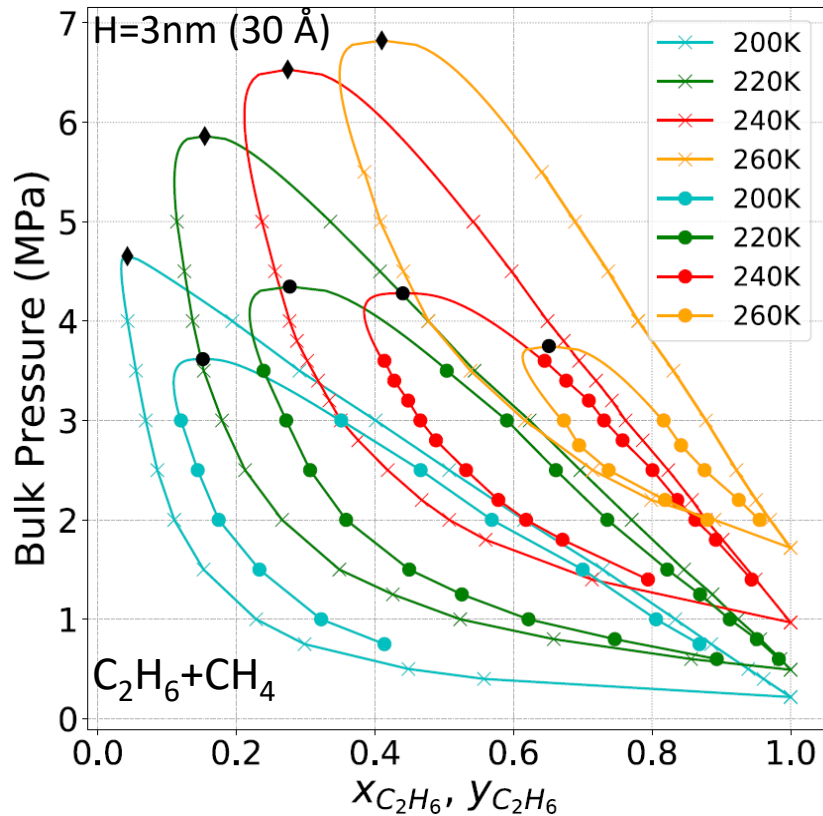
Bubble Point Monte Carlo



60% nC<sub>2</sub> + 40% nC<sub>5</sub> @  
3 nm graphite pore

## Confined GEMC NVT → @ high pressures close to Pc

# MIXTURE VLE UNDER CONFINEMENT



**Conclusion: Systematic reduction of the VLE with confinement**

**→  $T_c \downarrow$  &  $P_c \downarrow$  with reduction of pore size**

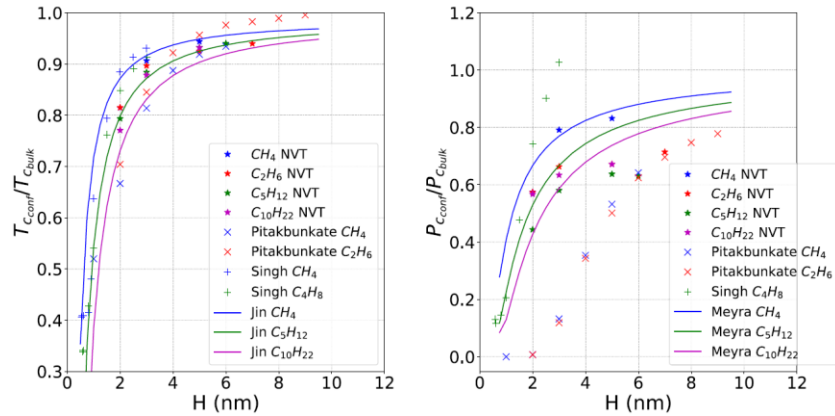
**→ Asymmetry between L or V in function of molecular affinity to the surface**

## EXTENSION TO LARGER LENGTH SCALES

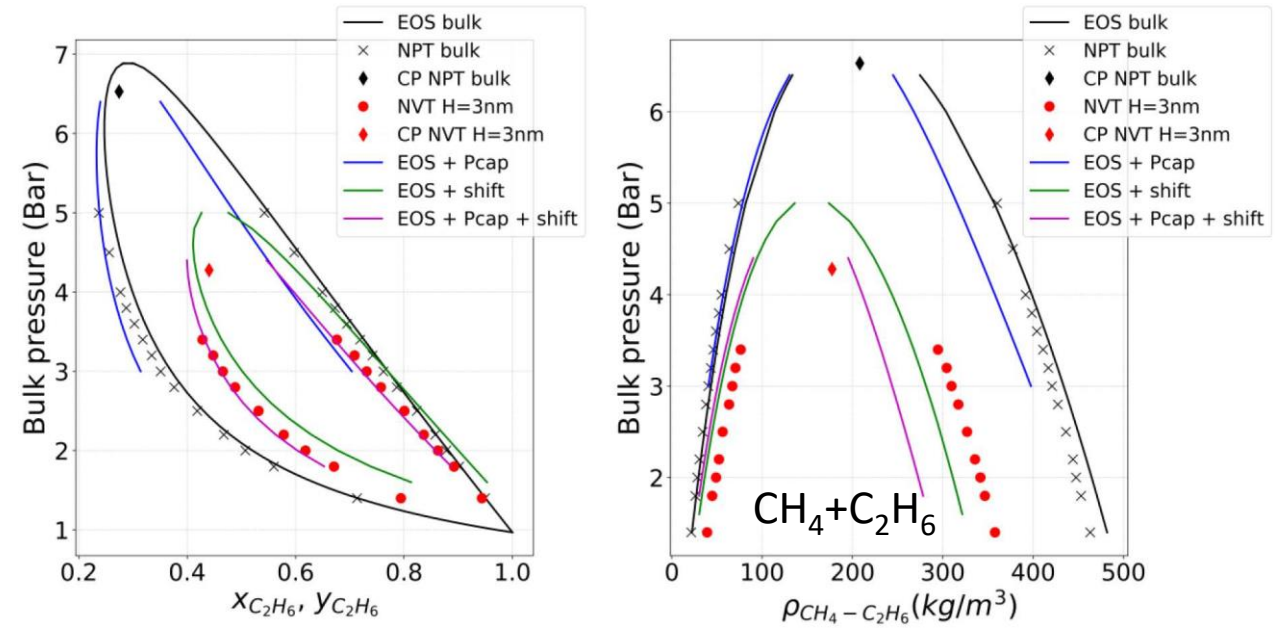
- How the information obtained from MS can be used ?
- To improve EoS (or adsorption models) to better include the confinement effect. Several approaches are possible (or combination of them):
  - Inclusion of capillary pressure ( $P_c$ )
  - Scaling of  $T_c$ ,  $P_c$  of pure components
  - Inclusion of the adsorbed phases & the cooperative effect (i.e., surfactants)
- Examples:
  - Phase behavior of hydrocarbons in non-conventional reservoirs simulations
    - Indirectly by using more accurate EoS with the effect of pore size ( $H$ )
    - Including the possibility to describe the heterogeneity of the media through local PSD
  - Surfactant adsorption modeling on mineral surfaces at mesoscales
    - Coarse grain simulation (DPD) → adsorption models → Lattice Boltzmann (LBM)

# IMPROVEMENT OF EOS

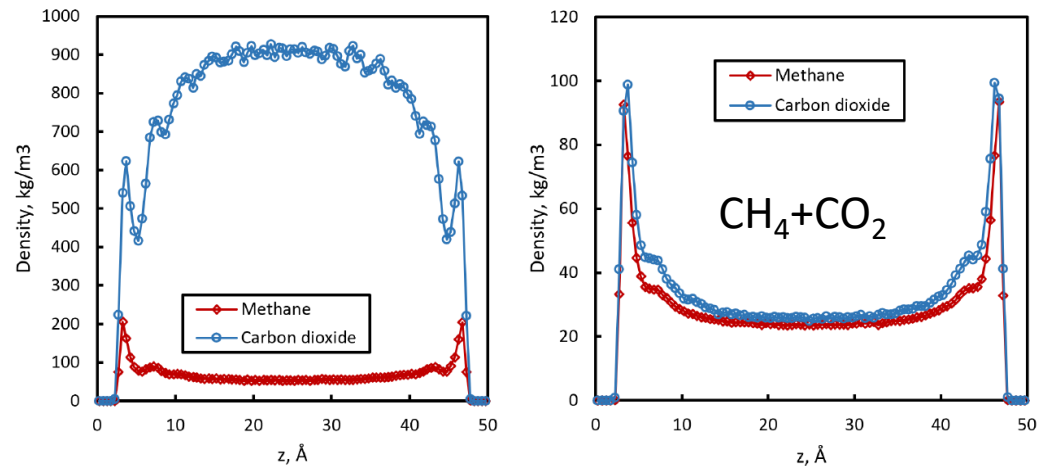
Providing correlations to model the variation of  $T_c$  (left) &  $P_c$  (right) with pore size



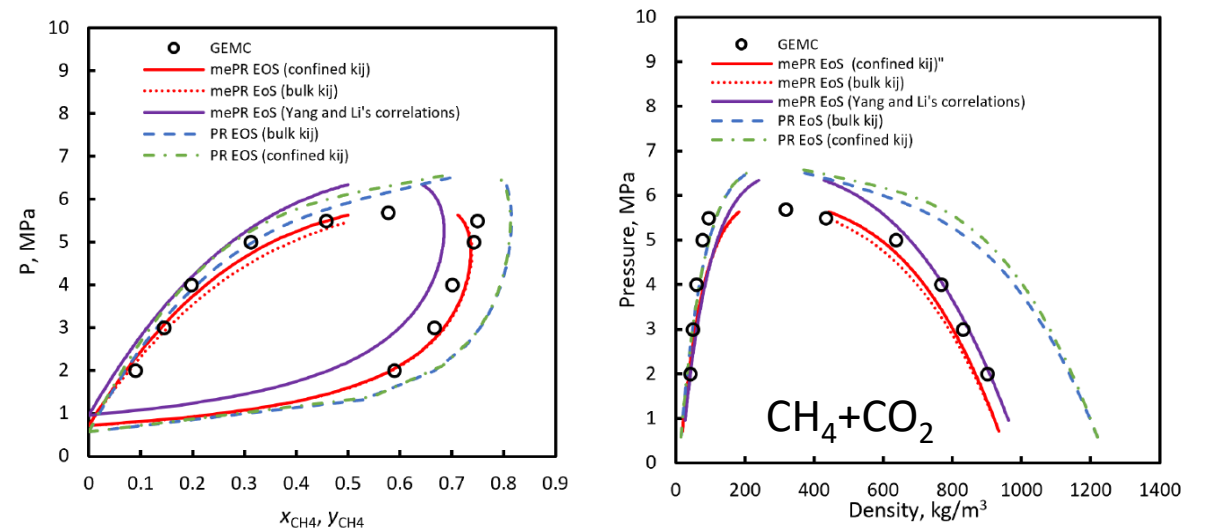
[2]



Providing additional information (local density profiles of pure & mixtures) on different phases



[3]



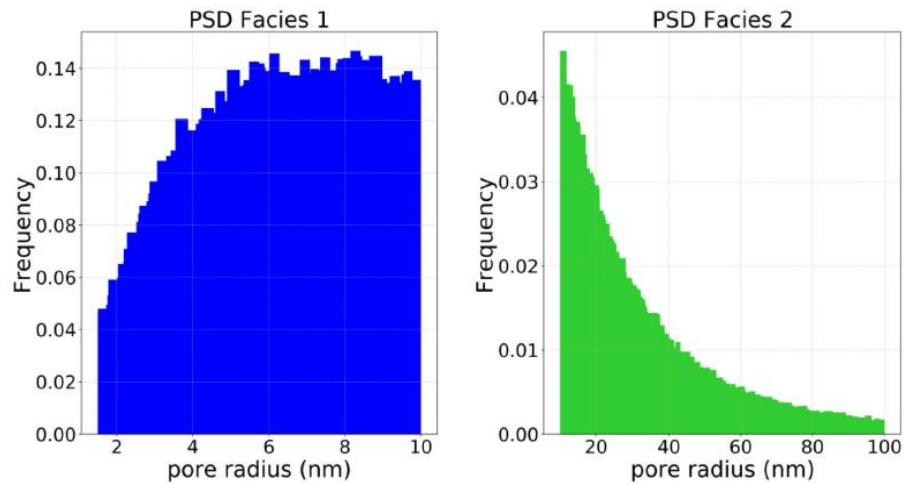
[1] Sobecki et al. Fluid Phase Equilib. 2019, 497, 104-121

[2] Sobecki et al. SPE-193867; J. Petrol. Sci. & Eng. 2020, 193, 107364

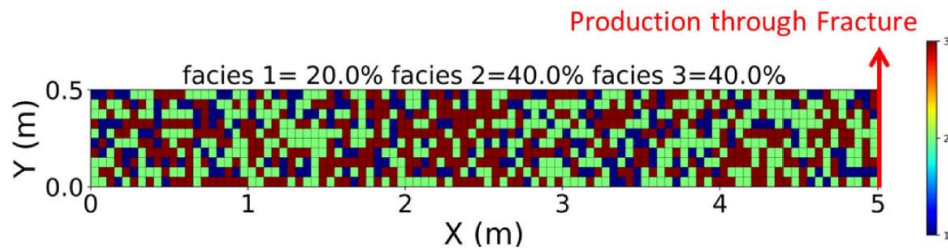
[3] Liu et al. J. Sup. Fluids 2022 (submitted)

# GRID MATRIX/FRACTURE PVT SIMULATION

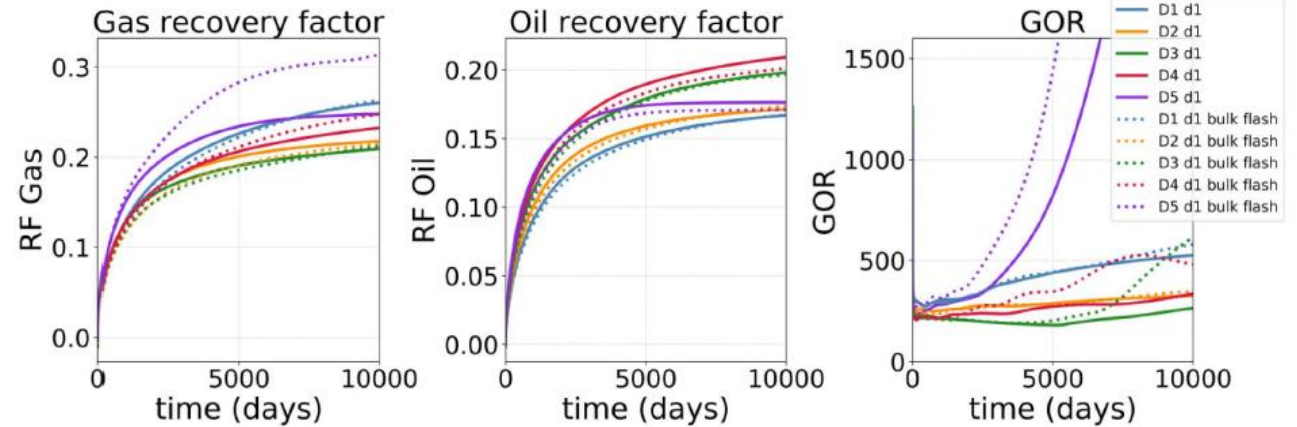
- Simulation of a fine grid including a pore size distribution (PSD) of different facies
- Influence of considering confinement in EoS on the Gas recovery factor, Oil recovery factor and Gas Oil Ratio (GOR)



Histogram of an example of PSD sample for facies 1 & 2



Example of one of the ten facies spatial distribution of D3 in the matrix

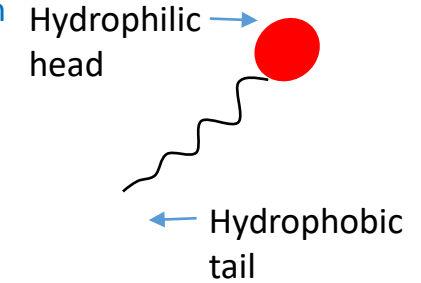
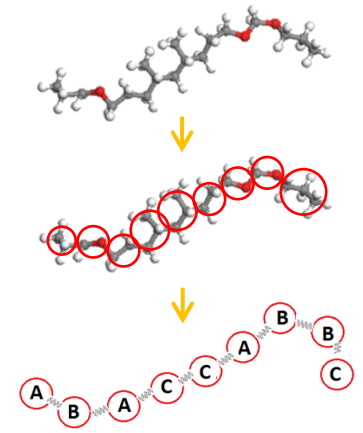


Distributions D1 & D3 have a negligible part of nanopores, modified PVT modelling has no strong impact on production for such distributions. However, D4 & D5 with higher percentage of nanopores, the difference between the two models is significant which mean that pore radius dependent EoS has an important impact on production for these distributions



# DISSIPATIVE PARTICLE DYNAMICS (DPD)

- Developed by Hoogerbrugge et Koelman in 1992. Stochastic simulation technique for simulating the dynamic and rheological properties of simple and complex fluids
- Particles represent whole molecules or fluid regions, rather than single atoms.
  - Particles or beads have the same volume  $v_m$ . In aqueous systems, the amount of water molecules/bead is used as the coarse graining level  $N_m$
- Calculations are done with **Newton** code<sup>1</sup> and the Slater screening charge implementation for Ewald sum.<sup>2</sup>
- Implementation of the protonation/deprotonation process through a Morse potential.<sup>3</sup>



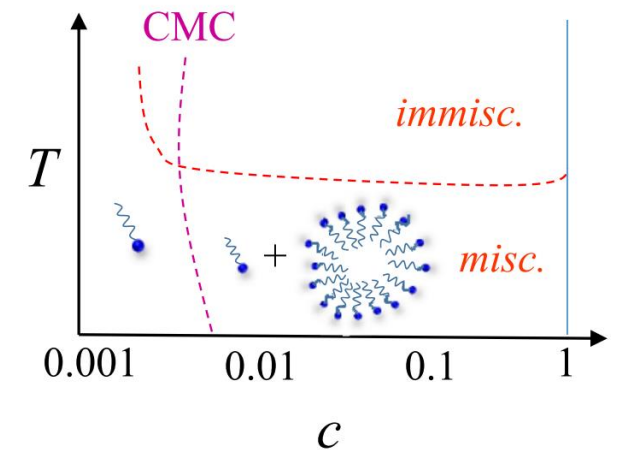
$$\frac{dr_i}{dt} = \mathbf{v}_i$$

$$m_i \frac{d\mathbf{v}_i}{dt} = \mathbf{f}_i$$

$$\mathbf{f}_i = m \frac{d\mathbf{v}_i}{dt} = \sum_{i \neq j} (\mathbf{F}_{ij}^C + \mathbf{F}_{ij}^D + \mathbf{F}_{ij}^R + \mathbf{F}_{ij}^S + \mathbf{F}_{ij}^{el} + \mathbf{F}_{ij}^M + \mathbf{F}_i^W + \mathbf{F}_i^{EW})$$

Conservative
Dissipative
Spring
Morse
Wall-bead Elec

Random
Electrostatics
Wall-bead vdW

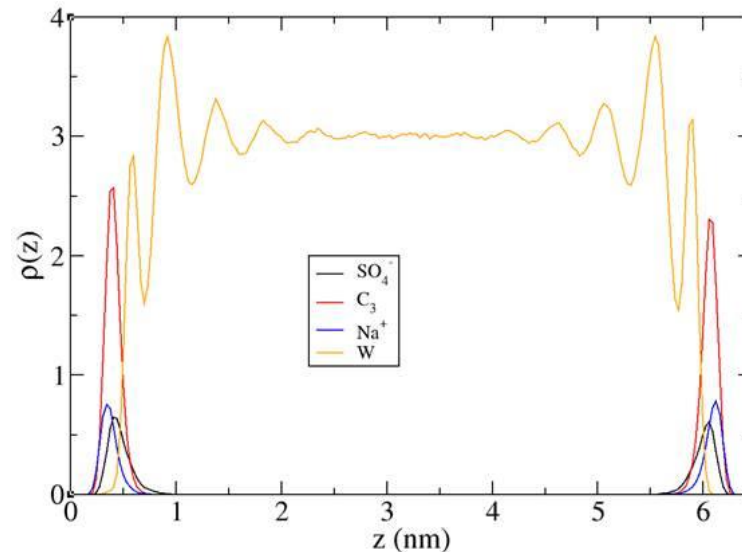
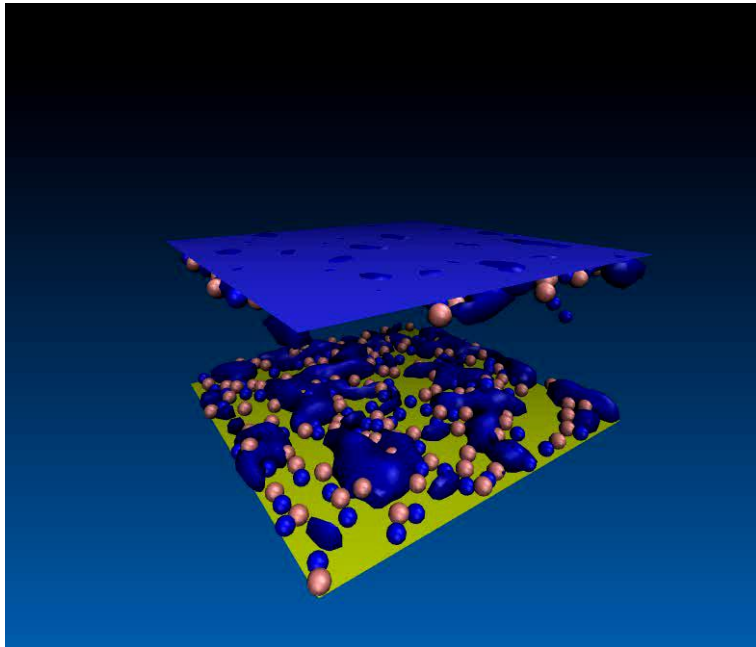


[1] PCCP 2010, 12 930.  
 [2] Gonzalez-Melchor et al. J. Chem. Phys. 2006, 125, 224107  
 [3] Lee et al. J. Chem. Theory Comput. 2015, 11, 4395–4403  
 [4] Alarcon et al. Soft. Matt. 2013, 9, 3777

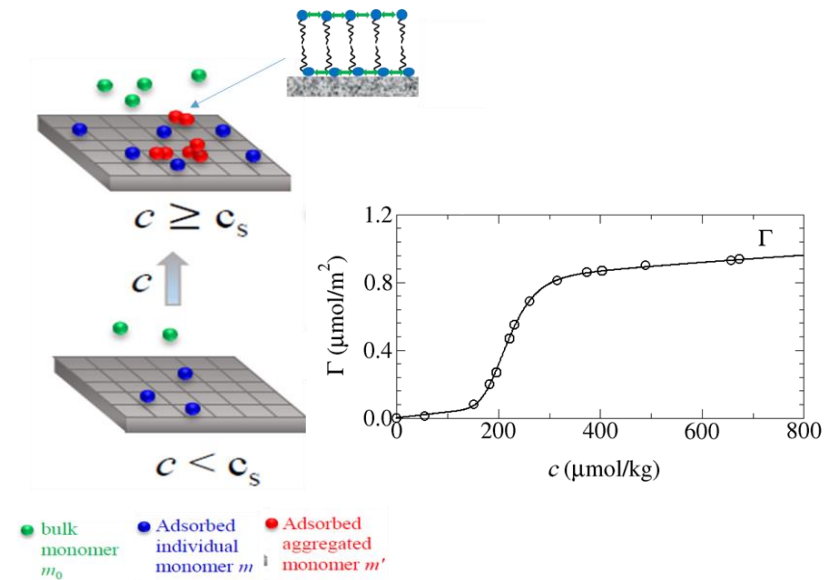
# ADSORPTION OF SURFACTANTS OVER MODEL-MINERAL SURFACES

- CG (DPD) model of charged surfactants (SNS =  $C_9H_{19}SO_4^- Na^+$ )  $H_1T_3$  Bulk  $[C]=0,308$  mol/l
- Hydrophobic  $SiO_2$  charged surface  $Q=600mC/m^2$  (Slit pore of  $l_x=13$  nm,  $l_y=13$  nm et  $l_z=6,5$  nm)

## Surface aggregation of surfactants



Surf.  $C_s=0,6$  molecules /  $nm^2$  or  $9,95 \times 10^{-7}$  mol/ $m^2$

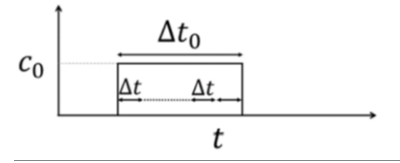


$$\frac{\partial \Gamma_m(c,t)}{\partial t} = k_{AC} [\Gamma^\infty - \Gamma_m(c,t)] - k_D \Gamma_m(c,t)$$

$$\frac{\partial \Gamma_{m'}(c,t)}{\partial t} = k'_A (\Gamma_{m'}) c \times [\Gamma^\infty - \Gamma_m(c,\infty) - \beta \Gamma_{m'}(c,t)] - k'_D (\Gamma_{m'}) \Gamma_{m'}(c,t)$$

Thermodynamic model of surfactant adsorption with surface aggregation and lateral interactions [1]

# TRANSPORT AND ADSORPTION MODELING USING LBM LANGMUIR VS COOPERATIVE MODEL: SLUG INJECTION



□ Lattice Boltzmann, Two-relaxation-Times scheme

□ 2D parallel plates geometry

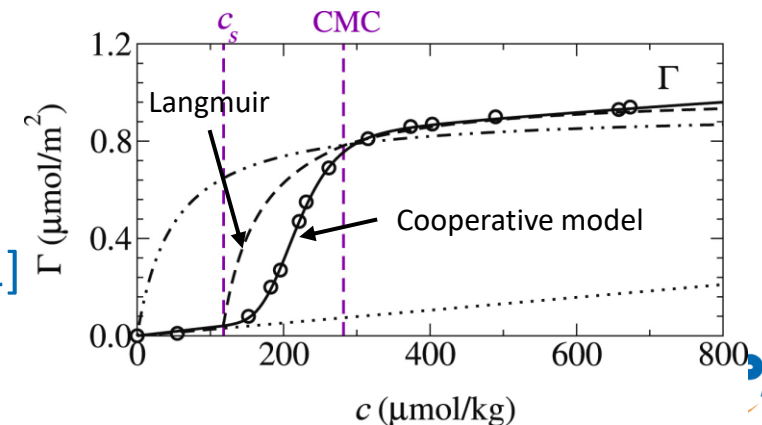
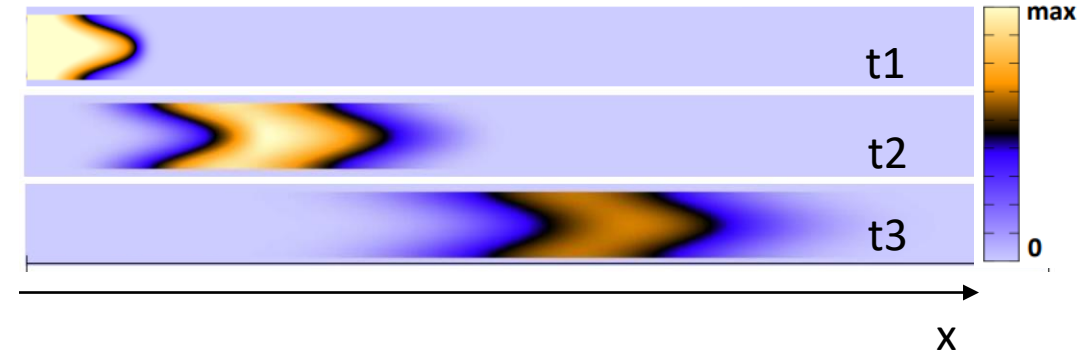
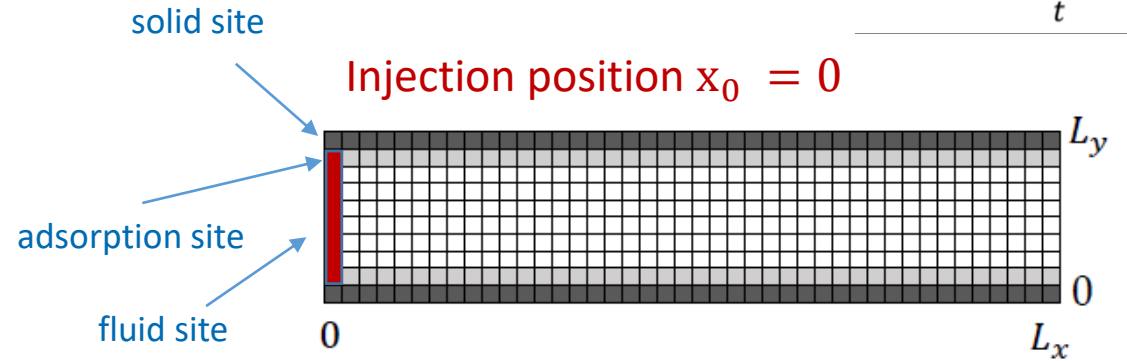
□ Two independent simulation steps

- Resolution of Stokes equation (velocity field)
- Resolution of the transport equation including the adsorption term

□ Initial conditions

- Dirac (pulse) injection ( $\Delta t=1$ )
- Continuous (slug) injection ( $\Delta t>1$ )

□ Langmuir model shows high adsorption for low surface saturation as it does not account for separated monomer and aggregate adsorption [1]



## CONCLUSIONS & PERSPECTIVES

- Molecular simulation techniques are well adapted to model the phase behavior of fluids under confinement & at interfaces if the contribution of fluid-solid interactions are of the same order of magnitude of “normal” fluid-fluid
  - This situation is observed in the case of microporosity (<2 nm) and in the lower limit of mesoporosity (2-10 nm)
  - Complex fluids capable of aggregation (surfactants)
- Experimental validation of the intermolecular force fields is crucial to keep the simulations as realistic as possible. Unfortunately, there is a lack of data in the literature of VLE of confined fluids.
- Advanced molecular/mesosopic simulation techniques (confined Gibbs ensemble MC, NPT-BPMC, DPD) can:
  - Enhance the comprehension of the behavior of fluids under strong confinement
  - provide valuable synthetic data to parametrize and validate modified EoS and thermodynamic adsorption models.
- The strategy of combining different multi-scale approaches is the most efficient way to inject the highest degree of physical & chemical coherence required to modeling of the complex phenomena involved in the phase behavior of confined fluids → LBM, grid matrix/fracture simulation.
- Challenges for the future:
  - Inclusion of more realistic models of mineral & heterogenous (cement) surfaces for the extension of the MS synthetic data for more realistic applications.
  - The inclusion of aqueous phases with high ionic concentrations in equilibrium with polar surfaces (Storage of H<sub>2</sub> in natural reservoirs)

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- Angela di Lella
- Nicolas Ferrando

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- Nicolas Sobecki @ RD EDF
- Zaineb Zaafouri

## ● @U. Grenoble/CNRS/LIPhy

- Benoît Coasne

## ● @Colorado School of Mines

- Shihao Wang
- Yu-Shu Wu

## ● @University of Wyoming

- Lingfu Liu
- Saman A. Aryana

## ● @University of São Paulo

- Ehsan Heidaryan



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